

**AMENDMENTS TO THE CLAIMS**

This listing of claims will replace all prior versions, and listings, of claims in the application:

Claims 1-30. (Cancelled)

31. (New) An automated method for frequency compensated communications reception including compensating for frequency offset in a received signal by adaptively forming a combination of basis functions and a training sequence that collectively approximate to a desired frequency-shifted signal to be acquired.
32. (New) A method according to Claim 31 including constructing a reference signal or comparison training sequence that is an adaptively formed combination of basis functions and the training sequence.
33. (New) A method according to Claim 32 for acquiring a signal with a receiver having multiple antenna elements, the method including constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a training sequence and a received signal, together with a constraint to obtain non-trivial solutions.
34. (New) A method according to Claim 33 wherein the constraint requires non-zero signal power.
35. (New) A method according to Claim 33 wherein the cost function is  $J$  given by:  
$$J = \|\mathbf{X}\mathbf{w} - \mathbf{C}\mathbf{F}\|^2 + \lambda(\mathbf{w}^H \mathbf{X}^H \mathbf{X} \mathbf{w} - 1)$$
, where  $\mathbf{X}$  is a matrix of received signal samples,  $\mathbf{w}$  is a vector of beamforming weights which are adaptive to minimise  $J$ ,  $\mathbf{C}$  is a

- diagonal matrix having elements of the training sequence on its diagonal,  $F$  is a matrix having columns defining respective basis functions,  $v$  is a vector of weights which are adaptive to minimise  $J$ , superscript index  $H$  indicates a complex conjugate transpose and  $\lambda$  is a Lagrange multiplier for a term to constrain beamformer output power to be non-zero.
36. (New) A method according to Claim 35 including determining the adaptive weight vectors  $w$  and  $v$  at intervals from true estimates of a correlation matrix determined from multiple data vectors and from inverses of such estimates recursively updated to reflect successive new data vectors which are rows of the matrix  $X$ .
37. (New) A method according to Claim 36 including recursively updating inverse correlation matrices by:
- forming a vector  $u(n)$  having a first element  $u_1(n)$  equal to  $\sqrt{U_{1,1}(n)}$  and other elements  $u_p(n)$  ( $p=2$  to  $M$ ) which are respective ratios  $U_{p,1}(n)/u_1(n)$ ,  $U_{p,1}(n)$  is a  $p$ th element of a first column of a matrix  $U(n)$ , the matrix  $U(n) \equiv u(n)u^H(n) = x(n)x^H(n) - x(n-K+1)x^H(n-K+1)$ ,  $x(n)$  is a most recent data vector and  $x(n-K+1)$  is a least recent data vector involved in updating and  $x(n)x^H(n)$  and  $x(n-K+1)x^H(n-K+1)$  are correlation matrices;
  - premultiplying a previous inverse correlation matrix  $P(n-1)$  by vector  $u^H(n)$  and postmultiplied by vector  $u(n)$  to form a product and adding the product to a forget factor to form a sum;
  - postmultiplying the previous inverse correlation matrix  $P(n-1)$  by vector  $u(n)$  and dividing by the said sum to form a quotient; and
  - subtracting the quotient from the previous inverse correlation matrix  $P(n-1)$  to provide a difference.

38. (New) A method according to Claim 32 for acquiring a signal with a receiver having a single antenna element, the method including constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a scaled received signal and a constraint requiring non-zero signal power.
39. (New) A method according to Claim 38 wherein the cost function is  $J$  given by:  
 $J = \|x - CFv\|^2$ , where  $x$  is a vector of received signal samples, and  $v$ ,  $C$  and  $F$  are as defined earlier.
40. (New) A method according to Claim 38 wherein the cost function is  $J$  given by:  
 $J = \|\alpha x - Gv\|^2 + \lambda(\alpha^* x^H x \alpha - 1)$ , where  $\alpha$  is a scaling factor,  $x$  is a vector of received signal samples,  $G$  is a matrix equal to  $CF$  and  $v$ ,  $\lambda$ ,  $C$ ,  $F$  and  $H$  are as defined earlier.
41. (New) Apparatus for frequency compensated communications reception including means for compensating for frequency offset in a received signal by adaptively forming a combination of basis functions and a training sequence that collectively approximate to a desired frequency-shifted signal to be acquired.
42. (New) Apparatus according to Claim 41 including means for constructing a reference signal or comparison training sequence that is an adaptively formed combination of basis functions and the training sequence.
43. (New) Apparatus according to Claim 42 having a receiver with multiple antenna elements for acquiring the received signal, the apparatus including means for constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a training sequence and a received signal, together with a constraint to obtain non-trivial solutions.

44. (New) Apparatus according to Claim 43 wherein the constraint requires non-zero signal power.
45. (New) Apparatus according to Claim 43 wherein the cost function is  $J$  given by:  

$$J = \|Xw - CFv\|^2 + \lambda(w^H X^H X w - 1)$$
, where  $X$  is a matrix of received signal samples,  $w$  is a vector of beamforming weights which are adaptive to minimise  $J$ ,  $C$  is a diagonal matrix having elements of the training sequence on its diagonal,  $F$  is a matrix having columns defining respective basis functions,  $v$  is a vector of weights which are adaptive to minimise  $J$ , superscript index  $H$  indicates a complex conjugate transpose and  $\lambda$  is a Lagrange multiplier for term to constrain beamformer output power to be non-zero.
46. (New) Apparatus according to Claim 45 including means for determining the adaptive weight vectors  $w$  and  $v$  at intervals from true estimates of a correlation matrix determined from multiple data vectors and from inverses of such estimates recursively updated to reflect successive new data vectors which are rows of the matrix  $X$ .
47. (New) Apparatus according to Claim 46 including means for recursively updating inverse correlation matrices by:
  - a) forming a vector  $u(n)$  having a first element  $u_1(n)$  equal to  $\sqrt{U_{1,1}(n)}$  and other elements  $u_p(n)$  ( $p=2$  to  $M$ ) which are respective ratios  $U_{p,1}(n)/u_1(n)$ ,  $U_{p,1}(n)$  is a  $p$ th element of a first column of a matrix  $U(n)$ , the matrix  $U(n) \equiv u(n)u^H(n) = x(n)x^H(n) - x(n-K+1)x^H(n-K+1)$ ,  $x(n)$  is a most recent data vector and  $x(n-K+1)$  is a least recent data vector involved in updating and  $x(n)x^H(n)$  and  $x(n-K+1)x^H(n-K+1)$  are correlation matrices;
  - b) premultiplying a previous inverse correlation matrix  $P(n-1)$  by vector  $u^H(n)$

- and postmultiplied by vector  $u(n)$  to form a product and adding the product to a forget factor to form a sum;
- c) postmultiplying the previous inverse correlation matrix  $P(n-1)$  by vector  $u(n)$  and dividing by the said sum to form a quotient; and
  - d) subtracting the quotient from the previous inverse correlation matrix  $P(n-1)$  to provide a difference.
48. (New) Apparatus according to Claim 42 having a receiver with a single antenna element for acquiring the received signal, the apparatus including means for constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a scaled received signal and a constraint requiring non-zero signal power.
49. (New) Apparatus according to Claim 48 wherein the cost function is  $J$  given by:  $J = \|x - CFv\|^2$ , where  $x$  is a vector of received signal samples, and  $v$ ,  $C$  and  $F$  are as defined earlier.
50. (New) Apparatus according to Claim 48 wherein the cost function is  $J$  given by:  $J = \|\alpha x - Gv\|^2 + \lambda(\alpha^* x^H x \alpha - 1)$ , where  $\alpha$  is a scaling factor,  $x$  is a vector of received signal samples,  $G$  is a matrix equal to  $CF$  and  $v$ ,  $\lambda$ ,  $C$ ,  $F$  and  $H$  are as defined earlier.
51. (New) A computer software product comprising a computer readable medium containing computer readable instructions for controlling operation of computer apparatus for use in frequency compensated communications reception, wherein the computer readable instructions provide a means for controlling the computer apparatus to compensate for frequency offset in a received signal by adaptively forming a combination of basis functions and a training sequence that collectively

approximate to a desired frequency-shifted signal to be acquired.

52. (New) A computer software product according to Claim 51 wherein the computer readable instructions provide a means for constructing a reference signal or comparison training sequence that is an adaptively formed combination of basis functions and the training sequence.
53. (New) A computer software product according to Claim 52 for use in processing received signals acquired by a receiver with multiple antenna elements, wherein the computer readable instructions provide a means for for constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a training sequence and a received signal, together with a constraint to obtain non-trivial solutions.
54. (New) A computer software product according to Claim 53 wherein the constraint requires non-zero signal power.
55. (New) A computer software product according to Claim 53 wherein the cost function is  $J$  given by:  $J = \|\mathbf{X}\mathbf{w} - \mathbf{C}\mathbf{F}\mathbf{v}\|^2 + \lambda(\mathbf{w}^H \mathbf{X}^H \mathbf{X} \mathbf{w} - 1)$ , where  $\mathbf{X}$  is a matrix of received signal samples,  $\mathbf{w}$  is a vector of beamforming weights which are adaptive to minimise  $J$ ,  $\mathbf{C}$  is a diagonal matrix having elements of the training sequence on its diagonal,  $\mathbf{F}$  is a matrix having columns defining respective basis functions,  $\mathbf{v}$  is a vector of weights which are adaptive to minimise  $J$ , superscript index  $H$  indicates a complex conjugate transpose and  $\lambda$  is a Lagrange multiplier and the term which incorporates it is to constrain beamformer output power to be non-zero.
56. (New) A computer software product according to Claim 55 wherein the computer readable instructions provide a means for determining the adaptive weight vectors  $\mathbf{w}$  and  $\mathbf{v}$  at intervals from true estimates of a correlation matrix

determined from multiple data vectors and from inverses of such estimates recursively updated to reflect successive new data vectors which are rows of the matrix  $X$ .

57. (New) A computer software product according to Claim 56 wherein the computer readable instructions provide a means for recursively updating inverse correlation matrices by:
- a) forming a vector  $u(n)$  having a first element  $u_1(n)$  equal to  $\sqrt{U_{1,1}(n)}$  and other elements  $u_p(n)$  ( $p=2$  to  $M$ ) which are respective ratios  $U_{p,1}(n)/u_1(n)$ ,  $U_{p,1}(n)$  is a  $p$ th element of a first column of a matrix  $U(n)$ , the matrix  $U(n) \equiv u(n)u^H(n) = x(n)x^H(n) - x(n-K+1)x^H(n-K+1)$ ,  $x(n)$  is a most recent data vector and  $x(n-K+1)$  is a least recent data vector involved in updating and  $x(n)x^H(n)$  and  $x(n-K+1)x^H(n-K+1)$  are correlation matrices;
  - b) premultiplying a previous inverse correlation matrix  $P(n-1)$  by vector  $u^H(n)$  and postmultiplied by vector  $u(n)$  to form a product and adding the product to a forget factor to form a sum;
  - c) postmultiplying the previous inverse correlation matrix  $P(n-1)$  by vector  $u(n)$  and dividing by the said sum to form a quotient; and
  - d) subtracting the quotient from the previous inverse correlation matrix  $P(n-1)$  to provide a difference.
58. (New) A computer software product according to Claim 52 for use in processing received signals acquired by a receiver with a single antenna element, wherein the computer readable instructions provide a means for constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a scaled received signal and a constraint requiring non-zero signal power.

59. (New) A computer software product according to Claim 58 wherein the cost function is  $J$  given by:  $J = \|x - CFv\|^2$ , where  $x$  is a vector of received signal samples, and  $v$ ,  $C$  and  $F$  are as defined earlier.
60. (New) A computer software product according to Claim 58 wherein the cost function is  $J$  given by:  $J = \|\alpha x - Gv\|^2 + \lambda(\alpha^* x^H x \alpha - 1)$ , where  $\alpha$  is a scaling factor,  $x$  is a vector of received signal samples,  $G$  is a matrix equal to  $CF$  and  $v$ ,  $\lambda$ ,  $C$ ,  $F$  and  $H$  are as defined earlier.